

## Index sets

$$\begin{aligned}
 COU &= \{COU1, COU2, COU3, COU4\} \\
 COUbig &= \{COU3, COU4\} \\
 COUf &= \{COU2, COU3, COU4\} \\
 COUh &= \{COU1\} \\
 COUonly &= \{COU1, COU2\} \\
 SEC &= \{SEC1, SEC2, SEC3, SEC4, SEC5, SEC6, SEC7, SEC8\} \\
 SECr &= \{SEC2, SEC3, SEC4, SEC5, SEC6, SEC7, SEC8\} \\
 SECnt &= \{SEC1, SEC2, SEC3, SEC4, SEC5, SEC6, SEC7\} \\
 SECr &= \{SEC1\} \\
 SEct &= \{SEC8\}
 \end{aligned}$$

## 1 CONSUMER $c \in COU$

### 1.1 Optimisation problem

$$\max_{(DD^{(c,s)})_{s \in SEC}, (DM^{(c,s)})_{s \in SEC}, (DT^{(c,s)})_{s \in SEC}} U^{CONS^{(c)}} = \left( \sum_{s \in SEC} \alpha^{dt^{(c,s)}} DT^{(c,s)} \sigma^{u^{(c)}-1} (-1 + \sigma^{u^{(c)}}) \right)^{\sigma^{u^{(c)}} (-1 + \sigma^{u^{(c)}})^{-1}} \quad (1.1)$$

s.t. :

$$INC^{CONS^{(c)}} = SV^{CONS^{(c)}} + \sum_{s \in SEC} p^{(c,s)} DD^{(c,s)} \left( 1 + tssj^{priv^{(c,s)}} \right) + \sum_{s \in SEC} p^{imp^{(c,s)}} DM^{(c,s)} \left( 1 + tssm^{priv^{(c,s)}} \right) \left( \lambda^{CONSUMER^1^{(c)}} \right) \quad (1.2)$$

$$s \in SEC: \quad DT^{(c,s)} = \left( \alpha^{dd^{(c,s)}} DD^{(c,s)} \sigma^{arm^{(c,s)}-1} (-1 + \sigma^{arm^{(c,s)}}) + \left( 1 - \alpha^{dd^{(c,s)}} \right) DM^{(c,s)} \sigma^{arm^{(c,s)}-1} (-1 + \sigma^{arm^{(c,s)}}) \right)^{\sigma^{arm^{(c,s)}} (-1 + \sigma^{arm^{(c,s)}})^{-1}} \left( \lambda^{CONSUMER^2^{(c,s)}} \right) \quad (1.3)$$

## 1.2 Identities

$$INC^{CONS\langle c \rangle} = -DEP\langle c \rangle + SUB\langle c \rangle + \phi\langle c \rangle PROFIT + p^{k\langle c \rangle} K\langle c \rangle \left(1 - \text{tinc}^{k\langle c \rangle}\right) + p^{l\langle c \rangle} L\langle c \rangle \left(1 - \text{tinc}^{l\langle c \rangle}\right) \quad (1.4)$$

$$INC^{CONS\langle c \rangle}^{-1} SV^{CONS\langle c \rangle} = \text{saving}^{\text{rate}^{CONS\langle c \rangle}} \quad (1.5)$$

$$DEP\langle c \rangle = \delta\langle c \rangle p^{k\langle c \rangle} K\langle c \rangle \quad (1.6)$$

$$L\langle c \rangle = \text{scale}\langle c \rangle^{-1} \left( -L^{\text{slack}\langle c \rangle} + \sum_{s \in SEC} L^{\text{data}\langle c, s \rangle} \right) \quad (1.7)$$

$$K\langle c \rangle = \text{scale}\langle c \rangle^{-1} \left( \sum_{s \in SEC} K^{\text{data}\langle c, s \rangle} \right) \quad (1.8)$$

## 1.3 First order conditions

$$s \in SEC: \quad \lambda^{\text{CONSUMER}^1\langle c \rangle} p^{\langle c, s \rangle} \left(1 + \text{tssl}^{\text{priv}\langle c, s \rangle}\right) + \alpha^{\text{dd}\langle c, s \rangle} \lambda^{\text{CONSUMER}^2\langle c, s \rangle} DD\langle c, s \rangle^{-1 + \sigma^{\text{arm}\langle c, s \rangle}} (-1 + \sigma^{\text{arm}\langle c, s \rangle})^{-1} \left( \alpha^{\text{dd}\langle c, s \rangle} DD\langle c, s \rangle \sigma^{\text{arm}\langle c, s \rangle} (-1 + \sigma^{\text{arm}\langle c, s \rangle})^{-1} \right) + \left(1 - \alpha^{\text{dd}\langle c, s \rangle}\right) DM\langle c, s \rangle \sigma^{\text{arm}\langle c, s \rangle} \quad (1.9)$$

$$\text{N} \quad s \in SEC: \quad \lambda^{\text{CONSUMER}^1\langle c \rangle} p^{\text{imp}\langle c, s \rangle} \left(1 + \text{tssm}^{\text{priv}\langle c, s \rangle}\right) + \lambda^{\text{CONSUMER}^2\langle c, s \rangle} \left(1 - \alpha^{\text{dd}\langle c, s \rangle}\right) DM\langle c, s \rangle^{-1 + \sigma^{\text{arm}\langle c, s \rangle}} (-1 + \sigma^{\text{arm}\langle c, s \rangle})^{-1} \left( \alpha^{\text{dd}\langle c, s \rangle} DD\langle c, s \rangle \sigma^{\text{arm}\langle c, s \rangle} (-1 + \sigma^{\text{arm}\langle c, s \rangle})^{-1} \right) + \left(1 - \alpha^{\text{dd}\langle c, s \rangle}\right) \quad (1.10)$$

$$s \in SEC: \quad -\lambda^{\text{CONSUMER}^2\langle c, s \rangle} + \alpha^{\text{dt}\langle c, s \rangle} DT\langle c, s \rangle^{-1 + \sigma^u\langle c \rangle} (-1 + \sigma^u\langle c \rangle)^{-1} \left( \sum_{s \in SEC} \alpha^{\text{dt}\langle c, s \rangle} DT\langle c, s \rangle \sigma^{u\langle c \rangle} (-1 + \sigma^u\langle c \rangle)^{-1} \right)^{-1 + \sigma^u\langle c \rangle} (-1 + \sigma^u\langle c \rangle)^{-1} = 0 \quad \left( DT\langle c, s \rangle \right) \quad (1.11)$$

$$r^{(c,s)} = p^{(c,s)} Y^{(c,s)} \left(1 - \text{trnd}^{(c,s)}\right) - p^k{}^{(c)} K^{(c,s)} \left(1 + \text{tjk}^{(c,s)}\right) - p^l{}^{(c)} L^{(c,s)} \left(1 + \text{tjl}^{(c,s)}\right) - \sum_{\text{si} \in \text{SEC}} p^{(c,\text{si})} \text{ICD}^{(c,s,\text{si})} \left(1 + \text{tssd}^{\text{prod}(c,s,\text{si})}\right) - \sum_{\text{si} \in \text{SEC}} p^{\text{imp}(c,\text{si})} \text{ICM}^{(c,s,\text{si})} \left(1 + \text{tssm}^{\text{prod}(c,s,\text{si})}\right) \quad (2.1)$$

$$\left. r^{(c,s)} \right|_{-1+\sigma^y(c,s)}^{-1} \left( -1 + \sigma^y(c,s) \right) \left. \right)^{\sigma^y(c,s) \left( -1 + \sigma^y(c,s) \right)^{-1}} \left( \lambda^{\text{FIRM}^1(c,s)} \right) \quad (2.2)$$

$$\left. r^{(c,s)} \right|_{-1+\sigma^{\text{fac}(c,s)}}^{-1} \left( -1 + \sigma^{\text{fac}(c,s)} \right) \left. \right)^{\sigma^{\text{fac}(c,s)} \left( -1 + \sigma^{\text{fac}(c,s)} \right)^{-1}} \left( \lambda^{\text{FIRM}^2(c,s)} \right) \quad (2.3)$$

$$\left( \lambda^{\text{FIRM}^3(c,s)} \right) \quad (2.4)$$

$$\left. r^{(c,s,\text{si})} \right|_{\text{ICM}^{(c,s,\text{si})} \sigma^{\text{arm}(c,\text{si})-1} \left( -1 + \sigma^{\text{arm}(c,\text{si})} \right)}^{-1} \left( -1 + \sigma^{\text{arm}(c,\text{si})} \right) \left. \right)^{\sigma^{\text{arm}(c,\text{si})} \left( -1 + \sigma^{\text{arm}(c,\text{si})} \right)^{-1}} \left( \lambda^{\text{FIRM}^4(c,s,\text{si})} \right) \quad (2.5)$$

$$\left. r^{(c,s)} \right|_{= p^{(c,s)} \left( 1 + \text{tee}^{(c,\alpha,s)} \right)} \quad (2.6)$$

$$\left. r^{(c,s)} \right|_{- \text{trnd}^{(c,s)}} = 0 \quad \left( Y^{(c,s)} \right) \quad (2.7)$$

$$\left. r^{(c,s)} \right|_{K^{(c,s)} \sigma^{\text{fac}(c,s)-1} \left( -1 + \sigma^{\text{fac}(c,s)} \right) + \left( 1 - \alpha^k(c,s) \right) L^{(c,s)} \sigma^{\text{fac}(c,s)-1} \left( -1 + \sigma^{\text{fac}(c,s)} \right)}^{-1} \left( -1 + \sigma^{\text{fac}(c,s)} \right) \left. \right)^{-1 + \sigma^{\text{fac}(c,s)} \left( -1 + \sigma^{\text{fac}(c,s)} \right)^{-1}} = 0 \quad \left( K^{(c,s)} \right) \quad (2.8)$$

$$\left. r^{(c,s)} \right|_{\alpha^k(c,s) K^{(c,s)} \sigma^{\text{fac}(c,s)-1} \left( -1 + \sigma^{\text{fac}(c,s)} \right) + \left( 1 - \alpha^k(c,s) \right) L^{(c,s)} \sigma^{\text{fac}(c,s)-1} \left( -1 + \sigma^{\text{fac}(c,s)} \right)}^{-1} \left( -1 + \sigma^{\text{fac}(c,s)} \right) \left. \right)^{-1 + \sigma^{\text{fac}(c,s)} \left( -1 + \sigma^{\text{fac}(c,s)} \right)^{-1}} = 0 \quad \left( L^{(c,s)} \right) \quad (2.9)$$



### 3 IMPORT BIG $c \in COU$ big $s \in SEC$

#### 3.1 Optimisation problem

$$\max_{(IM^{\langle \alpha, c, s \rangle})_{\alpha \in COU}, IMPORT^{\langle c, s \rangle}} \pi^{\text{imp}^{\langle c, s \rangle}} = p^{\text{imp}^{\langle c, s \rangle}} IMPORT^{\langle c, s \rangle} - \text{scale}^{\langle c \rangle - 1} \left( \sum_{\alpha \in COU} \text{scale}^{\langle \alpha \rangle} p^{\text{cif}^{\langle \alpha, c, s \rangle}} IM^{\langle \alpha, c, s \rangle} \left( 1 + \text{trm}^{\langle \alpha, c, s \rangle} \right) \right) \quad (3.1)$$

s.t. :

$$IMPORT^{\langle c, s \rangle} = \theta^{\text{im}^{\langle c, s \rangle}} \left( \sum_{\alpha \in COU} \alpha^{\text{im}^{\langle \alpha, c, s \rangle}} \left( \text{scale}^{\langle c \rangle - 1} \text{scale}^{\langle \alpha \rangle} IM^{\langle \alpha, c, s \rangle} \left( 1 + \text{itberg}^{\text{cost}^{\langle \alpha, c, s \rangle}} \right) \right)^{\sigma^{\text{im}^{\langle s \rangle} - 1} (-1 + \sigma^{\text{im}^{\langle s \rangle}})} \right)^{\sigma^{\text{im}^{\langle s \rangle}} (-1 + \sigma^{\text{im}^{\langle s \rangle}})^{-1}} \left( \lambda^{\text{IMPORT}^{\text{BIG}^1 \langle c, s \rangle}} \right) \quad (3.2)$$

#### 3.2 Identities

$$\alpha \in COU: \quad IM^{\langle \alpha, c, s \rangle} = EX^{\langle \alpha, c, s \rangle} \quad (3.3)$$

$$\alpha \in COU: \quad p^{\text{cif}^{\langle c, \alpha, s \rangle}} = p^{\text{fob}^{\langle c, \alpha, s \rangle}} + \tau^{\langle c, \alpha, s \rangle} p^{\text{trans}} \quad (3.4)$$

#### 3.3 First order conditions

$$\alpha \in COU: \quad -\text{scale}^{\langle c \rangle - 1} \text{scale}^{\langle \alpha \rangle} p^{\text{cif}^{\langle \alpha, c, s \rangle}} \left( 1 + \text{trm}^{\langle \alpha, c, s \rangle} \right) + \alpha^{\text{im}^{\langle \alpha, c, s \rangle}} \text{scale}^{\langle c \rangle - 1} \text{scale}^{\langle \alpha \rangle} \theta^{\text{im}^{\langle c, s \rangle}} \lambda^{\text{IMPORT}^{\text{BIG}^1 \langle c, s \rangle}} \left( 1 + \text{itberg}^{\text{cost}^{\langle \alpha, c, s \rangle}} \right) \left( \text{scale}^{\langle c \rangle - 1} \text{scale}^{\langle \alpha \rangle} IM^{\langle \alpha, c, s \rangle} \left( 1 + \text{itberg}^{\text{cost}^{\langle \alpha, c, s \rangle}} \right) \right)^{-1 + \sigma^{\text{im}^{\langle s \rangle}}} = 0 \quad (3.5)$$

$$-\lambda^{\text{IMPORT}^{\text{BIG}^1 \langle c, s \rangle}} + p^{\text{imp}^{\langle c, s \rangle}} = 0 \quad \left( IMPORT^{\langle c, s \rangle} \right) \quad (3.6)$$

#### 3.4 First order conditions after reduction

$$\alpha \in COU: \quad -\text{scale}^{\langle c \rangle - 1} \text{scale}^{\langle \alpha \rangle} p^{\text{cif}^{\langle \alpha, c, s \rangle}} \left( 1 + \text{trm}^{\langle \alpha, c, s \rangle} \right) + \alpha^{\text{im}^{\langle \alpha, c, s \rangle}} \text{scale}^{\langle c \rangle - 1} \text{scale}^{\langle \alpha \rangle} \theta^{\text{im}^{\langle c, s \rangle}} p^{\text{imp}^{\langle c, s \rangle}} \left( 1 + \text{itberg}^{\text{cost}^{\langle \alpha, c, s \rangle}} \right) \left( \text{scale}^{\langle c \rangle - 1} \text{scale}^{\langle \alpha \rangle} IM^{\langle \alpha, c, s \rangle} \left( 1 + \text{itberg}^{\text{cost}^{\langle \alpha, c, s \rangle}} \right) \right)^{-1 + \sigma^{\text{im}^{\langle s \rangle}}} = 0 \quad (3.7)$$

## 4 IMPORT SMALL $c \in COU$ only $s \in SEC$

### 4.1 Optimisation problem

$$\max_{(IM^{\langle \alpha, c, s \rangle})_{\alpha \in COU \setminus c}, IMPORT^{\langle c, s \rangle}} \pi^{\text{imp}^{\langle c, s \rangle}} = p^{\text{imp}^{\langle c, s \rangle}} IMPORT^{\langle c, s \rangle} - \text{scale}^{\langle c \rangle}{}^{-1} \left( \sum_{\alpha \in COU} \text{scale}^{\langle \alpha \rangle} p^{\text{cif}^{\langle \alpha, c, s \rangle}} IM^{\langle \alpha, c, s \rangle} \left( 1 + \text{trm}^{\langle \alpha, c, s \rangle} \right) \right) \quad (4.1)$$

s.t. :

$$IMPORT^{\langle c, s \rangle} = \theta^{\text{im}^{\langle c, s \rangle}} \left( \sum_{\alpha \in COU \setminus c} \alpha^{\text{im}^{\langle \alpha, c, s \rangle}} \left( \text{scale}^{\langle c \rangle}{}^{-1} \text{scale}^{\langle \alpha \rangle} IM^{\langle \alpha, c, s \rangle} \left( 1 + \text{iceberg}^{\text{cost}^{\langle \alpha, c, s \rangle}} \right) \right)^{\sigma^{\text{im}^{\langle s \rangle}} - 1} \left( -1 + \sigma^{\text{im}^{\langle s \rangle}} \right) \right)^{\sigma^{\text{im}^{\langle s \rangle}} \left( -1 + \sigma^{\text{im}^{\langle s \rangle}} \right)^{-1}} \left( \lambda^{\text{IMPORT}^{\text{SMALL}^1 \langle c, s \rangle}} \right) \quad (4.2)$$

### 4.2 Identities

$$\alpha \in COU: \quad IM^{\langle \alpha, c, s \rangle} = EX^{\langle \alpha, c, s \rangle} \quad (4.3)$$

$$\text{scale}^{\langle c \rangle} IM^{\langle c, c, s \rangle} = 0 \quad (4.4)$$

$$\alpha \in COU: \quad p^{\text{cif}^{\langle c, \alpha, s \rangle}} = p^{\text{fob}^{\langle c, \alpha, s \rangle}} + \tau^{\langle c, \alpha, s \rangle} p^{\text{trans}} \quad (4.5)$$

### 4.3 First order conditions

$$\alpha \in COU \setminus c: \quad -\text{scale}^{\langle c \rangle}{}^{-1} \left( \sum_{\alpha' \in COU} \delta^{\langle \alpha, \alpha' \rangle} \text{scale}^{\langle \alpha' \rangle} p^{\text{cif}^{\langle \alpha', c, s \rangle}} \left( 1 + \text{trm}^{\langle \alpha', c, s \rangle} \right) \right) + \alpha^{\text{im}^{\langle \alpha, c, s \rangle}} \text{scale}^{\langle c \rangle}{}^{-1} \text{scale}^{\langle \alpha \rangle} \theta^{\text{im}^{\langle c, s \rangle}} \lambda^{\text{IMPORT}^{\text{SMALL}^1 \langle c, s \rangle}} \left( 1 + \text{iceberg}^{\text{cost}^{\langle \alpha, c, s \rangle}} \right) \left( \text{scale}^{\langle c \rangle}{}^{-1} \text{scale}^{\langle \alpha \rangle} IM^{\langle \alpha, c, s \rangle} \right) \quad (4.6)$$

$$-\lambda^{\text{IMPORT}^{\text{SMALL}^1 \langle c, s \rangle}} + p^{\text{imp}^{\langle c, s \rangle}} = 0 \quad (IMPORT^{\langle c, s \rangle}) \quad (4.7)$$

### 4.4 First order conditions after reduction

$$\alpha \in COU \setminus c: \quad -\text{scale}^{\langle c \rangle}{}^{-1} \left( \sum_{\alpha' \in COU} \delta^{\langle \alpha, \alpha' \rangle} \text{scale}^{\langle \alpha' \rangle} p^{\text{cif}^{\langle \alpha', c, s \rangle}} \left( 1 + \text{trm}^{\langle \alpha', c, s \rangle} \right) \right) + \alpha^{\text{im}^{\langle \alpha, c, s \rangle}} \text{scale}^{\langle c \rangle}{}^{-1} \text{scale}^{\langle \alpha \rangle} \theta^{\text{im}^{\langle c, s \rangle}} p^{\text{imp}^{\langle c, s \rangle}} \left( 1 + \text{iceberg}^{\text{cost}^{\langle \alpha, c, s \rangle}} \right) \left( \text{scale}^{\langle c \rangle}{}^{-1} \text{scale}^{\langle \alpha \rangle} IM^{\langle \alpha, c, s \rangle} \left( 1 + \text{iceberg}^{\text{cost}^{\langle \alpha, c, s \rangle}} \right) \right) \quad (4.8)$$

## 5 GOVERNMENT $c \in COU$

### 5.1 Optimisation problem

$$\max_{(GT^{(c,s)})_{s \in SEC}, (GD^{(c,s)})_{s \in SEC}, (GM^{(c,s)})_{s \in SEC}} U^{GOV^{(c)}} = \prod_{s \in SEC} GT^{(c,s) \beta^{gov^{(c,s)}}} \quad (5.1)$$

s.t. :

$$s \in SEC: \quad GT^{(c,s)} = \left( \alpha^{gt^{(c,s)}} GD^{(c,s) \sigma^{arm^{(c,s)} - 1} (-1 + \sigma^{arm^{(c,s)}})} + (1 - \alpha^{gt^{(c,s)}}) GM^{(c,s) \sigma^{arm^{(c,s)} - 1} (-1 + \sigma^{arm^{(c,s)}})} \right)^{\sigma^{arm^{(c,s)}} (-1 + \sigma^{arm^{(c,s)}})^{-1}} \left( \lambda^{GOVERNMENT^1^{(c,s)}} \right) \quad (5.2)$$

$$INC^{GOV^{(c)}} - SUB^{(c)} = \sum_{s \in SEC} p^{(c,s)} GD^{(c,s)} \left( 1 + tssd^{gov^{(c,s)}} \right) + \sum_{s \in SEC} p^{imp^{(c,s)}} GM^{(c,s)} \left( 1 + tssm^{gov^{(c,s)}} \right) \quad \left( \lambda^{GOVERNMENT^2^{(c)}} \right) \quad (5.3)$$

### 5.2 Identities

$$INC^{GOV^{(c)}} = Tee^{(c)} + Tfk^{(c)} + Tf^1^{(c)} + Tirc^{(c)} + Tmm^{(c)} + Tprod^{(c)} + Tssm^{(c)} + Tssd^{(c)} \quad (5.4)$$

$$SUB^{(c)} = gsub^{(c)} INC^{GOV^{(c)}} \quad (5.5)$$

$$Tmm^{(c)} = scale^{(c) - 1} \left( \sum_{s \in SEC} \sum_{\alpha \in COU} scale^{(\alpha)} tmm^{(\alpha, c, s)} p^{cif^{(\alpha, c, s)}} IM^{(\alpha, c, s)} \right) \quad (5.6)$$

$$Tee^{(c)} = \sum_{s \in SEC} p^{(c,s)} \left( \sum_{\alpha \in COU} tee^{(c, \alpha, s)} EX^{(c, \alpha, s)} \right) \quad (5.7)$$

$$Tssm^{(c)} = \sum_{s \in SEC} p^{imp^{(c,s)}} \left( tssm^{priv^{(c,s)}} DM^{(c,s)} + tssm^{gov^{(c,s)}} GM^{(c,s)} + tssm^{cgds^{(c,s)}} CM^{(c,s)} + \sum_{si \in SEC} tssm^{prod^{(c, si, s)}} ICM^{(c, si, s)} \right) \quad (5.8)$$

$$Tssd^{(c)} = \sum_{s \in SEC} p^{(c,s)} \left( tssd^{priv^{(c,s)}} DD^{(c,s)} + tssd^{gov^{(c,s)}} GD^{(c,s)} + tssd^{cgds^{(c,s)}} CD^{(c,s)} + \sum_{si \in SEC} tssd^{prod^{(c, si, s)}} ICD^{(c, si, s)} \right) \quad (5.9)$$

$$Tfk^{(c)} = p^k^{(c)} \left( \sum_{s \in SEC} tfk^{(c,s)} K^{(c,s)} \right) \quad (5.10)$$

$$Tf^1^{(c)} = p^1^{(c)} \left( \sum_{s \in SEC} tf^1^{(c,s)} L^{(c,s)} \right) \quad (5.11)$$

$$T_{prod}^{(c)} = \sum_{s \in SEC} t_{prod}^{(c,s)} p^{(c,s)} Y^{(c,s)} \quad (5.12)$$

$$T_{inc}^{(c)} = t_{inc}^{k(c)} p^{k(c)} K^{(c)} + t_{inc}^{1(c)} p^{1(c)} L^{(c)} \quad (5.13)$$

### 5.3 First order conditions

$$s \in SEC: \quad -\lambda^{GOVERNMENT^1(c,s)} + \beta^{gov(c,s)} GT^{(c,s)-1} \left( \prod_{s' \in SEC} GT^{(c,s')} \beta^{gov(c,s')} \right) = 0 \quad (GT^{(c,s)}) \quad (5.14)$$

$$s \in SEC: \quad \lambda^{GOVERNMENT^2(c)} p^{(c,s)} \left( 1 + t_{ssd}^{gov(c,s)} \right) + \alpha^{gt(c,s)} \lambda^{GOVERNMENT^1(c,s)} GD^{(c,s)-1+\sigma^{arm(c,s)-1}(-1+\sigma^{arm(c,s)})} \left( \alpha^{gt(c,s)} GD^{(c,s)\sigma^{arm(c,s)-1}(-1+\sigma^{arm(c,s)})} + (1 - \alpha^{gt(c,s)}) GM^{(c,s)} \right) \quad (5.15)$$

$$s \in SEC: \quad \lambda^{GOVERNMENT^2(c)} p^{imp(c,s)} \left( 1 + t_{ssm}^{gov(c,s)} \right) + \lambda^{GOVERNMENT^1(c,s)} \left( 1 - \alpha^{gt(c,s)} \right) GM^{(c,s)-1+\sigma^{arm(c,s)-1}(-1+\sigma^{arm(c,s)})} \left( \alpha^{gt(c,s)} GD^{(c,s)\sigma^{arm(c,s)-1}(-1+\sigma^{arm(c,s)})} + (1 - \alpha^{gt(c,s)}) \right) \quad (5.16)$$

## 6 TRANSPORT

∞

### 6.1 Optimisation problem

$$TRANS^{global}, (TRANS^{total(c)})_{c \in COU} \quad \max \quad \pi^{trans} = p^{trans} TRANS^{global} - \sum_{c \in COU} p^{(c, SEC8)} TRANS^{total(c)} \quad (6.1)$$

s.t. :

$$TRANS^{global} = \theta^{trans} \left( \prod_{c \in COU} TRANS^{total(c)} \beta^{trans(c)} \right) \quad (\lambda^{TRANSPORT^1}) \quad (6.2)$$

### 6.2 Identities

$$c \in COU: \quad \alpha \in COU: \quad TRANS^{(c,\alpha)} = scale^{(c)} scale^{(\alpha)-1} \left( \sum_{s \in SEC} \tau^{(c,\alpha,s)} IM^{(c,\alpha,s)} \right) \quad (6.3)$$

$$c \in COU \setminus \{COU4\}: \quad TRANS^{total(c)} = -TRANS^{bal(c)} + \sum_{\alpha \in COU} TRANS^{(c,\alpha)} \quad (6.4)$$

$$\sum_{c \in COU} TRANS^{bal(c)} = 0 \quad (6.5)$$



### 6.3 First order conditions

$$-\lambda^{\text{TRANSPORT}^1} + p^{\text{trans}} = 0 \quad \left( \text{TRANS}^{\text{global}} \right) \quad (6.6)$$

$$c \in \text{COU}: \quad -p^{\langle c, \text{SEC8} \rangle} + \theta^{\text{trans}} \beta^{\text{trans} \langle c \rangle} \lambda^{\text{TRANSPORT}^1} \text{TRANS}^{\text{total} \langle c \rangle - 1} \left( \prod_{c' \in \text{COU}} \text{TRANS}^{\text{total} \langle c' \rangle \beta^{\text{trans} \langle c' \rangle}} \right) = 0 \quad \left( \text{TRANS}^{\text{total} \langle c \rangle} \right) \quad (6.7)$$

### 6.4 First order conditions after reduction

$$c \in \text{COU}: \quad -p^{\langle c, \text{SEC8} \rangle} + \theta^{\text{trans}} \beta^{\text{trans} \langle c \rangle} p^{\text{trans}} \text{TRANS}^{\text{total} \langle c \rangle - 1} \left( \prod_{c' \in \text{COU}} \text{TRANS}^{\text{total} \langle c' \rangle \beta^{\text{trans} \langle c' \rangle}} \right) = 0 \quad \left( \left( \text{TRANS}^{\text{total} \langle c \rangle} \right)_{c \in \text{COU}} \right) \quad (6.8)$$

## 7 BANK

### 7.1 Optimisation problem

$$\max_{\left( \text{INV}^{\langle c \rangle} \right)_{c \in \text{COU}}, \left( \text{CT}^{\langle c, s \rangle} \right)_{s \in \text{SEC}}_{c \in \text{COU}}, \left( \text{CD}^{\langle c, s \rangle} \right)_{s \in \text{SEC}}_{c \in \text{COU}}, \left( \text{CM}^{\langle c, s \rangle} \right)_{s \in \text{SEC}}_{c \in \text{COU}}} \text{INVEST} = \theta^{\text{invest}} \left( \prod_{c \in \text{COU}} \text{INV}^{\langle c \rangle \beta^{\text{invest} \langle c \rangle}} \right) \quad (7.1)$$

s.t. :

$$\text{SAVINGS} = \sum_{c \in \text{COU}} \sum_{s \in \text{SEC}} p^{\langle c, s \rangle} \text{CD}^{\langle c, s \rangle} \left( 1 + \text{tssd}^{\text{cgds} \langle c, s \rangle} \right) + \sum_{c \in \text{COU}} \sum_{s \in \text{SEC}} p^{\text{imp} \langle c, s \rangle} \text{CM}^{\langle c, s \rangle} \left( 1 + \text{tssm}^{\text{cgds} \langle c, s \rangle} \right) \quad \left( \lambda^{\text{BANK}^1} \right) \quad (7.2)$$

$$c \in \text{COU}: \quad \text{INV}^{\langle c \rangle} = \theta^{\text{inv} \langle c \rangle} \left( \prod_{s \in \text{SEC}} \text{CT}^{\langle c, s \rangle \beta^{\text{inv} \langle c, s \rangle}} \right) \quad \left( \lambda^{\text{BANK}^2 \langle c \rangle} \right) \quad (7.3)$$

$$c \in \text{COU}: \quad s \in \text{SEC}: \quad \text{CT}^{\langle c, s \rangle} = \theta^{\text{ct} \langle c, s \rangle} \left( \alpha^{\text{ct} \langle c, s \rangle} \text{CD}^{\langle c, s \rangle \sigma^{\text{arm} \langle c, s \rangle - 1} (-1 + \sigma^{\text{arm} \langle c, s \rangle})} + (1 - \alpha^{\text{ct} \langle c, s \rangle}) \text{CM}^{\langle c, s \rangle \sigma^{\text{arm} \langle c, s \rangle - 1} (-1 + \sigma^{\text{arm} \langle c, s \rangle})} \right) \sigma^{\text{arm} \langle c, s \rangle (-1 + \sigma^{\text{arm} \langle c, s \rangle})^{-1}} \quad \left( \lambda^{\text{BANK}^3 \langle s, c \rangle} \right) \quad (7.4)$$

### 7.2 Identities

$$\text{SAVINGS} = \sum_{c \in \text{COU}} \text{SV}^{\text{REG} \langle c \rangle} \quad (7.5)$$

$$c \in \text{COU}: \quad \text{SV}^{\text{REG} \langle c \rangle} = -\text{CA}^{\langle c \rangle} + \text{DEP}^{\langle c \rangle} + \text{SV}^{\text{CONS} \langle c \rangle} + p^{\langle c, \text{SEC8} \rangle} \text{TRANS}^{\text{bal} \langle c \rangle} \quad (7.6)$$

$$\alpha \in \text{COU}: \quad \text{CA}^{\langle \alpha \rangle} = - \sum_{\alpha \in \text{COU}} \text{EX}^{\text{bal} \langle \alpha, \alpha \rangle} \quad (7.7)$$

$$c \in COU: \quad \alpha \in COU: \quad scale^{(c)} EX^{bal^{(c,\alpha)}} = scale^{(\alpha)} \left( \sum_{s \in SEC} p^{fob^{(c,\alpha,s)}} IM^{(\alpha,c,s)} \right) - scale^{(c)} \left( \sum_{s \in SEC} p^{fob^{(c,\alpha,s)}} EX^{(c,\alpha,s)} \right) \quad (7.8)$$

### 7.3 First order conditions

$$c \in COU: \quad -\lambda^{BANK^2^{(c)}} + \theta^{invest} \beta^{invest^{(c)}} INV^{(c)-1} \left( \prod_{c' \in COU} INV^{(c')} \beta^{invest^{(c')}} \right) = 0 \quad (INV^{(c)}) \quad (7.9)$$

$$c \in COU: \quad s \in SEC: \quad -\lambda^{BANK^3^{(s,c)}} + \beta^{inv^{(c,s)}} \theta^{inv^{(c)}} \lambda^{BANK^2^{(c)}} CT^{(c,s)-1} \left( \prod_{s' \in SEC} CT^{(c,s')} \beta^{inv^{(c,s')}} \right) = 0 \quad (CT^{(c,s)}) \quad (7.10)$$

$$c \in COU: \quad s \in SEC: \quad \lambda^{BANK^1} p^{(c,s)} \left( 1 + tssd^{cgds^{(c,s)}} \right) + \alpha^{ct^{(c,s)}} \theta^{ct^{(c,s)}} \lambda^{BANK^3^{(s,c)}} CD^{(c,s)-1+\sigma^{arm^{(c,s)}}-1(-1+\sigma^{arm^{(c,s)}})} \left( \alpha^{ct^{(c,s)}} CD^{(c,s)\sigma^{arm^{(c,s)}}-1(-1+\sigma^{arm^{(c,s)}})} + (1 - \alpha^{ct^{(c,s)}}) CM^{(c,s)} \right) \quad (7.11)$$

$$c \in COU: \quad s \in SEC: \quad \lambda^{BANK^1} p^{imp^{(c,s)}} \left( 1 + tssm^{cgds^{(c,s)}} \right) + \theta^{ct^{(c,s)}} \lambda^{BANK^3^{(s,c)}} \left( 1 - \alpha^{ct^{(c,s)}} \right) CM^{(c,s)-1+\sigma^{arm^{(c,s)}}-1(-1+\sigma^{arm^{(c,s)}})} \left( \alpha^{ct^{(c,s)}} CD^{(c,s)\sigma^{arm^{(c,s)}}-1(-1+\sigma^{arm^{(c,s)}})} + (1 - \alpha^{ct^{(c,s)}}) \right) \quad (7.12)$$

10

## 8 EQUILIBRIUM

### 8.1 Identities

$$c \in COU: \quad s \in SEC: \quad Y^{home^{(c,s)}} = CD^{(c,s)} + DD^{(c,s)} + GD^{(c,s)} + \sum_{\hat{s} \in SEC} ICD^{(c,\hat{s},s)} \quad (8.1)$$

$$c \in COU: \quad s \in SECT: \quad Y^{(c,s)} = Y^{home^{(c,s)}} + \sum_{\alpha \in COU} EX^{(c,\alpha,s)} \quad (8.2)$$

$$c \in COU: \quad s \in SECT: \quad Y^{(c,s)} = TRANS^{total^{(c)}} + Y^{home^{(c,s)}} + \sum_{\alpha \in COU} EX^{(c,\alpha,s)} \quad (8.3)$$

$$c \in COU: \quad s \in SEC: \quad IMPORT^{(c,s)} = CM^{(c,s)} + DM^{(c,s)} + GM^{(c,s)} + \sum_{\hat{s} \in SEC} ICM^{(c,\hat{s},s)} \quad (8.4)$$

$$c \in COU: \quad K^{(c)} = \sum_{s \in SEC} K^{(c,s)} \quad (8.5)$$

$$c \in COU: \quad L^{(c)} = \sum_{s \in SEC} L^{(c,s)} \quad (8.6)$$

$$\left( \sum_{c \in COU} K^{(c)} + \sum_{c \in COU} L^{(c)} \right)^{-1} \left( \sum_{c \in COU} p^{k(c)} K^{(c)} + \sum_{c \in COU} p^{l(c)} L^{(c)} \right) = 1 \quad (8.7)$$

$$PROFIT = \pi^{\text{trans}} + \sum_{c \in COU} \sum_{s \in SEC} \pi^{(c,s)} + \sum_{c \in COU} \sum_{s \in SEC} \pi^{\text{imp}(c,s)} \quad (8.8)$$

## 9 Equilibrium relationships (before expansion and reduction)

$$- \sum_{c \in COU} TRANS^{\text{bal}(c)} = 0 \quad (9.1)$$

$$1 - \left( \sum_{c \in COU} K^{(c)} + \sum_{c \in COU} L^{(c)} \right)^{-1} \left( \sum_{c \in COU} p^{k(c)} K^{(c)} + \sum_{c \in COU} p^{l(c)} L^{(c)} \right) = 0 \quad (9.2)$$

$$INVEST - \theta^{\text{invest}} \left( \prod_{c \in COU} INV^{(c)\beta^{\text{invest}(c)}} \right) = 0 \quad (9.3)$$

$$-SAVINGS + \sum_{c \in COU} SV^{\text{REG}(c)} = 0 \quad (9.4)$$

$$-TRANS^{\text{global}} + \theta^{\text{trans}} \left( \prod_{c \in COU} TRANS^{\text{total}(c)\beta^{\text{trans}(c)}} \right) = 0 \quad (9.5)$$

$$\pi^{\text{trans}} - p^{\text{trans}} TRANS^{\text{global}} + \sum_{c \in COU} p^{(c, \text{SEC8})} TRANS^{\text{total}(c)} = 0 \quad (9.6)$$

$$-SAVINGS + \sum_{c \in COU} \sum_{s \in SEC} p^{(c,s)} CD^{(c,s)} \left( 1 + tssl^{\text{cgds}(c,s)} \right) + \sum_{c \in COU} \sum_{s \in SEC} p^{\text{imp}(c,s)} CM^{(c,s)} \left( 1 + tssm^{\text{cgds}(c,s)} \right) = 0 \quad (9.7)$$

$$\pi^{\text{trans}} - PROFIT + \sum_{c \in COU} \sum_{s \in SEC} \pi^{(c,s)} + \sum_{c \in COU} \sum_{s \in SEC} \pi^{\text{imp}(c,s)} = 0 \quad (9.8)$$

$$c \in COU \setminus \{COU4\}: \quad -TRANS^{\text{total}(c)} - TRANS^{\text{bal}(c)} + \sum_{\alpha \in COU} TRANS^{(\alpha,c)} = 0 \quad (9.9)$$

$$c \in COU: \quad \text{saving}^{\text{rate}^{\text{cons}(c)}} - INC^{\text{CONS}(c)-1} SV^{\text{CONS}(c)} = 0 \quad (9.10)$$

$$c \in COU: \quad -\lambda^{\text{BANK}^2(c)} + \theta^{\text{invest}} \beta^{\text{invest}(c)} INV^{(c)-1} \left( \prod_{c' \in COU} INV^{(c')\beta^{\text{invest}(c')}} \right) = 0 \quad (9.11)$$

$$c \in COU: \quad -p^{(c, SEC8)} + \theta^{trans} \beta^{trans(c)} p^{trans} TRANS^{total(c)-1} \left( \prod_{c' \in COU} TRANS^{total(c')} \beta^{trans(c')} \right) = 0 \quad (9.12)$$

$$\alpha \in COU: \quad -CA^{(\alpha)} - \sum_{\alpha \in COU} EX^{bal(\alpha, \alpha)} = 0 \quad (9.13)$$

$$c \in COU: \quad -DEP^{(c)} + \delta^{(c)} p^k(c) K^{(c)} = 0 \quad (9.14)$$

$$c \in COU: \quad -INV^{(c)} + \theta^{inv(c)} \left( \prod_{s \in SEC} CT^{(c,s)} \beta^{inv(c,s)} \right) = 0 \quad (9.15)$$

$$c \in COU: \quad -K^{(c)} + scale^{(c)-1} \left( \sum_{s \in SEC} K^{data(c,s)} \right) = 0 \quad (9.16)$$

$$c \in COU: \quad -K^{(c)} + \sum_{s \in SEC} K^{(c,s)} = 0 \quad (9.17)$$

$$c \in COU: \quad -L^{(c)} + scale^{(c)-1} \left( -L^{slack(c)} + \sum_{s \in SEC} L^{data(c,s)} \right) = 0 \quad (9.18)$$

$$c \in COU: \quad -L^{(c)} + \sum_{s \in SEC} L^{(c,s)} = 0 \quad (9.19)$$

$$c \in COU: \quad -SUB^{(c)} + gsub^{(c)} INC^{GOV(c)} = 0 \quad (9.20)$$

$$c \in COU: \quad -Tee^{(c)} + \sum_{s \in SEC} p^{(c,s)} \left( \sum_{\alpha \in COU} tee^{(c,\alpha,s)} EX^{(c,\alpha,s)} \right) = 0 \quad (9.21)$$

$$c \in COU: \quad -Tf^k(c) + p^k(c) \left( \sum_{s \in SEC} tf^k(c,s) K^{(c,s)} \right) = 0 \quad (9.22)$$

$$c \in COU: \quad -Tf^1(c) + p^1(c) \left( \sum_{s \in SEC} tf^1(c,s) L^{(c,s)} \right) = 0 \quad (9.23)$$

$$c \in COU: \quad -Tmm^{(c)} + scale^{(c)-1} \left( \sum_{s \in SEC} \sum_{\alpha \in COU} scale^{(\alpha)} tmm^{(\alpha,c,s)} p^{cif(\alpha,c,s)} IM^{(\alpha,c,s)} \right) = 0 \quad (9.24)$$

$$c \in COU: \quad -Tpral^{(c)} + \sum_{s \in SEC} tpral^{(c,s)} p^{(c,s)} Y^{(c,s)} = 0 \quad (9.25)$$

$$c \in COU: \quad -Tssm^{(c)} + \sum_{s \in SEC} p^{\text{imp}(c,s)} \left( tssm^{\text{priv}(c,s)} DM^{(c,s)} + tssm^{\text{gov}(c,s)} GM^{(c,s)} + tssm^{\text{cgds}(c,s)} CM^{(c,s)} + \sum_{\tilde{s} \in SEC} tssm^{\text{prod}(c,\tilde{s},s)} ICM^{(c,\tilde{s},s)} \right) = 0 \quad (9.26)$$

$$c \in COU: \quad -Tssd^{(c)} + \sum_{s \in SEC} p^{(c,s)} \left( tssd^{\text{priv}(c,s)} DD^{(c,s)} + tssd^{\text{gov}(c,s)} GD^{(c,s)} + tssd^{\text{cgds}(c,s)} CD^{(c,s)} + \sum_{\tilde{s} \in SEC} tssd^{\text{prod}(c,\tilde{s},s)} ICD^{(c,\tilde{s},s)} \right) = 0 \quad (9.27)$$

$$c \in COU: \quad U^{\text{CONS}(c)} - \left( \sum_{s \in SEC} \alpha^{\text{dt}(c,s)} DT^{(c,s)} \sigma^{u(c)-1} (-1 + \sigma^{u(c)}) \right)^{\sigma^{u(c)} (-1 + \sigma^{u(c)})^{-1}} = 0 \quad (9.28)$$

$$c \in COU: \quad U^{\text{GOV}(c)} - \prod_{s \in SEC} GT^{(c,s)} \beta^{\text{gov}(c,s)} = 0 \quad (9.29)$$

$$c \in COU: \quad -Tinc^{(c)} + tinc^k{}^{(c)} p^k{}^{(c)} K^{(c)} + tinc^1{}^{(c)} p^1{}^{(c)} L^{(c)} = 0 \quad (9.30)$$

$$c \in COU: \quad -INC^{\text{GOV}(c)} + SUB^{(c)} + \sum_{s \in SEC} p^{(c,s)} GD^{(c,s)} (1 + tssd^{\text{gov}(c,s)}) + \sum_{s \in SEC} p^{\text{imp}(c,s)} GM^{(c,s)} (1 + tssm^{\text{gov}(c,s)}) = 0 \quad (9.31)$$

$$c \in COU: \quad -INC^{\text{CONS}(c)} + SV^{\text{CONS}(c)} + \sum_{s \in SEC} p^{(c,s)} DD^{(c,s)} (1 + tssd^{\text{priv}(c,s)}) + \sum_{s \in SEC} p^{\text{imp}(c,s)} DM^{(c,s)} (1 + tssm^{\text{priv}(c,s)}) = 0 \quad (9.32)$$

$$c \in COU: \quad -CA^{(c)} + DEP^{(c)} + SV^{\text{CONS}(c)} - SV^{\text{REG}(c)} + p^{(c,SEC8)} TRANS^{\text{bal}(c)} = 0 \quad (9.33)$$

$$c \in COU: \quad -DEP^{(c)} - INC^{\text{CONS}(c)} + SUB^{(c)} + \phi^{(c)} PROFIT + p^k{}^{(c)} K^{(c)} (1 - tinc^k{}^{(c)}) + p^1{}^{(c)} L^{(c)} (1 - tinc^1{}^{(c)}) = 0 \quad (9.34)$$

$$c \in COU: \quad -INC^{\text{GOV}(c)} + Tte^{(c)} + Tfk^{(c)} + Tfl^{(c)} + Tinc^{(c)} + Tmm^{(c)} + Tprod^{(c)} + Tssm^{(c)} + Tssd^{(c)} = 0 \quad (9.35)$$

$$c \in COU: \quad \alpha \in COU: \quad -TRANS^{(c,\alpha)} + scale^{(c)} scale^{(\alpha)-1} \left( \sum_{s \in SEC} \tau^{(c,\alpha,s)} IM^{(c,\alpha,s)} \right) = 0 \quad (9.36)$$

$$c \in COU: \quad \alpha \in COU: \quad -scale^{(c)} \left( \sum_{s \in SEC} p^{\text{fob}(c,\alpha,s)} EX^{(c,\alpha,s)} \right) + scale^{(\alpha)} \left( \sum_{s \in SEC} p^{\text{fob}(\alpha,c,s)} IM^{(\alpha,c,s)} \right) - scale^{(c)} EX^{\text{bal}(c,\alpha)} = 0 \quad (9.37)$$

$$c \in COU: \quad s \in SEC: \quad -\lambda^{\text{CONSUMER}^2(c,s)} + \alpha^{\text{dt}(c,s)} DT^{(c,s)} \sigma^{u(c)-1} (-1 + \sigma^{u(c)}) \left( \sum_{s \in SEC} \alpha^{\text{dt}(c,s)} DT^{(c,s)} \sigma^{u(c)-1} (-1 + \sigma^{u(c)}) \right)^{-1 + \sigma^{u(c)} (-1 + \sigma^{u(c)})^{-1}} = 0 \quad (9.38)$$

$$c \in COU: \quad s \in SEC: \quad -\lambda^{\text{GOVERNMENT}^1(c,s)} + \beta^{\text{gov}(c,s)} GT^{(c,s)} \beta^{\text{gov}(c,s)}^{-1} \left( \prod_{s' \in SEC} GT^{(c,s')} \beta^{\text{gov}(c,s')} \right) = 0 \quad (9.39)$$

$$c \in COU: \quad s \in SEC: \quad -\lambda^{\text{BANK}^3(s,c)} + \beta^{\text{inv}(c,s)} \theta^{\text{inv}(c)} \lambda^{\text{BANK}^2(c)} CT^{(c,s)} \beta^{\text{inv}(c,s)}^{-1} \left( \prod_{s' \in SEC} CT^{(c,s')} \beta^{\text{inv}(c,s')} \right) = 0 \quad (9.40)$$

$$c \in COU: \quad s \in SEC: \quad -CT^{(c,s)} + \theta^{ct(c,s)} \left( \alpha^{ct(c,s)} CD^{(c,s)} \sigma^{\text{arm}(c,s)-1} (-1 + \sigma^{\text{arm}(c,s)}) + \left( 1 - \alpha^{ct(c,s)} \right) CM^{(c,s)} \sigma^{\text{arm}(c,s)-1} (-1 + \sigma^{\text{arm}(c,s)}) \right) \sigma^{\text{arm}(c,s)} (-1 + \sigma^{\text{arm}(c,s)})^{-1} = 0 \quad (9.41)$$

$$c \in COU: \quad s \in SEC: \quad -DT^{(c,s)} + \left( \alpha^{dd(c,s)} DD^{(c,s)} \sigma^{\text{arm}(c,s)-1} (-1 + \sigma^{\text{arm}(c,s)}) + \left( 1 - \alpha^{dd(c,s)} \right) DM^{(c,s)} \sigma^{\text{arm}(c,s)-1} (-1 + \sigma^{\text{arm}(c,s)}) \right) \sigma^{\text{arm}(c,s)} (-1 + \sigma^{\text{arm}(c,s)})^{-1} = 0 \quad (9.42)$$

$$c \in COU: \quad s \in SEC: \quad -FAC^{(c,s)} + \left( \alpha^{k(c,s)} K^{(c,s)} \sigma^{\text{fac}(c,s)-1} (-1 + \sigma^{\text{fac}(c,s)}) + \left( 1 - \alpha^{k(c,s)} \right) L^{(c,s)} \sigma^{\text{fac}(c,s)-1} (-1 + \sigma^{\text{fac}(c,s)}) \right) \sigma^{\text{fac}(c,s)} (-1 + \sigma^{\text{fac}(c,s)})^{-1} = 0 \quad (9.43)$$

$$c \in COU: \quad s \in SEC: \quad -GT^{(c,s)} + \left( \alpha^{gt(c,s)} GD^{(c,s)} \sigma^{\text{arm}(c,s)-1} (-1 + \sigma^{\text{arm}(c,s)}) + \left( 1 - \alpha^{gt(c,s)} \right) GM^{(c,s)} \sigma^{\text{arm}(c,s)-1} (-1 + \sigma^{\text{arm}(c,s)}) \right) \sigma^{\text{arm}(c,s)} (-1 + \sigma^{\text{arm}(c,s)})^{-1} = 0 \quad (9.44)$$

$$c \in COU: \quad s \in SEC: \quad -IC^{(c,s)} + \left( \sum_{\tilde{s} \in SEC} \alpha^{ict(c,s,\tilde{s})} ICT^{(c,s,\tilde{s})} \sigma^{ic(c,s)-1} (-1 + \sigma^{ic(c,s)}) \right) \sigma^{ic(c,s)} (-1 + \sigma^{ic(c,s)})^{-1} = 0 \quad (9.45)$$

$$c \in COU: \quad s \in SEC: \quad -Y^{(c,s)} + tfp^{y(c,s)} \left( \alpha^{\text{fac}(c,s)} FAC^{(c,s)} \sigma^{y(c,s)-1} (-1 + \sigma^{y(c,s)}) + \left( 1 - \alpha^{\text{fac}(c,s)} \right) IC^{(c,s)} \sigma^{y(c,s)-1} (-1 + \sigma^{y(c,s)}) \right) \sigma^{y(c,s)} (-1 + \sigma^{y(c,s)})^{-1} = 0 \quad (9.46)$$

14

$$c \in COU: \quad s \in SEC: \quad -p^{k(c)} \left( 1 + tf^{k(c,s)} \right) + \alpha^{\text{fac}(c,s)} \alpha^{k(c,s)} tfp^{y(c,s)} p^{(c,s)} \left( 1 - \text{tr}^{d(c,s)} \right) FAC^{(c,s)-1} \sigma^{y(c,s)-1} (-1 + \sigma^{y(c,s)}) K^{(c,s)-1} \sigma^{\text{fac}(c,s)-1} (-1 + \sigma^{\text{fac}(c,s)}) \left( \alpha^{\text{fac}(c,s)} FAC^{(c,s)} \sigma^{y(c,s)-1} \right) \quad (9.47)$$

$$c \in COU: \quad s \in SEC: \quad -p^{l(c)} \left( 1 + tf^{l(c,s)} \right) + \alpha^{\text{fac}(c,s)} tfp^{y(c,s)} p^{(c,s)} \left( 1 - \alpha^{k(c,s)} \right) \left( 1 - \text{tr}^{d(c,s)} \right) FAC^{(c,s)-1} \sigma^{y(c,s)-1} (-1 + \sigma^{y(c,s)}) L^{(c,s)-1} \sigma^{\text{fac}(c,s)-1} (-1 + \sigma^{\text{fac}(c,s)}) \left( \alpha^{\text{fac}(c,s)} FAC^{(c,s)} \sigma^{y(c,s)-1} \right) \quad (9.48)$$

$$c \in COU: \quad s \in SEC: \quad \lambda^{\text{BANK}^1} p^{(c,s)} \left( 1 + \text{tssd}^{\text{cgds}(c,s)} \right) + \alpha^{ct(c,s)} \theta^{ct(c,s)} \lambda^{\text{BANK}^3(s,c)} CD^{(c,s)-1} \sigma^{\text{arm}(c,s)-1} (-1 + \sigma^{\text{arm}(c,s)}) \left( \alpha^{ct(c,s)} CD^{(c,s)} \sigma^{\text{arm}(c,s)-1} (-1 + \sigma^{\text{arm}(c,s)}) + \left( 1 - \alpha^{ct(c,s)} \right) CM^{(c,s)} \right) \quad (9.49)$$

$$c \in COU: \quad s \in SEC: \quad \lambda^{\text{BANK}^1} p^{\text{imp}(c,s)} \left( 1 + \text{tssm}^{\text{cgds}(c,s)} \right) + \theta^{ct(c,s)} \lambda^{\text{BANK}^3(s,c)} \left( 1 - \alpha^{ct(c,s)} \right) CM^{(c,s)-1} \sigma^{\text{arm}(c,s)-1} (-1 + \sigma^{\text{arm}(c,s)}) \left( \alpha^{ct(c,s)} CD^{(c,s)} \sigma^{\text{arm}(c,s)-1} (-1 + \sigma^{\text{arm}(c,s)}) + \left( 1 - \alpha^{ct(c,s)} \right) CM^{(c,s)} \right) \quad (9.50)$$

$$c \in COU: \quad s \in SEC: \quad \lambda^{\text{CONSUMER}^1(c)} p^{(c,s)} \left( 1 + \text{tssd}^{\text{priv}(c,s)} \right) + \alpha^{dd(c,s)} \lambda^{\text{CONSUMER}^2(c,s)} DD^{(c,s)-1} \sigma^{\text{arm}(c,s)-1} (-1 + \sigma^{\text{arm}(c,s)}) \left( \alpha^{dd(c,s)} DD^{(c,s)} \sigma^{\text{arm}(c,s)-1} (-1 + \sigma^{\text{arm}(c,s)}) + \left( 1 - \alpha^{dd(c,s)} \right) DM^{(c,s)} \right) \quad (9.51)$$

$$c \in COU: \quad s \in SEC: \quad \lambda^{\text{CONSUMER}^1(c)} p^{\text{imp}(c,s)} \left( 1 + \text{tssm}^{\text{priv}(c,s)} \right) + \lambda^{\text{CONSUMER}^2(c,s)} \left( 1 - \alpha^{dd(c,s)} \right) DM^{(c,s)-1} \sigma^{\text{arm}(c,s)-1} (-1 + \sigma^{\text{arm}(c,s)}) \left( \alpha^{dd(c,s)} DD^{(c,s)} \sigma^{\text{arm}(c,s)-1} (-1 + \sigma^{\text{arm}(c,s)}) + \left( 1 - \alpha^{dd(c,s)} \right) DM^{(c,s)} \right) \quad (9.52)$$

$$c \in COU: \quad s \in SEC: \quad \lambda^{\text{GOVERNMENT}^2 \langle c \rangle} p^{\langle c, s \rangle} \left( 1 + tssd^{\text{gov} \langle c, s \rangle} \right) + \alpha^{\text{gt} \langle c, s \rangle} \lambda^{\text{GOVERNMENT}^1 \langle c, s \rangle} GD^{\langle c, s \rangle - 1 + \sigma^{\text{arm} \langle c, s \rangle - 1} (-1 + \sigma^{\text{arm} \langle c, s \rangle})} \left( \alpha^{\text{gt} \langle c, s \rangle} GD^{\langle c, s \rangle \sigma^{\text{arm} \langle c, s \rangle - 1} (-1 + \sigma^{\text{arm} \langle c, s \rangle})} + (1 - \alpha^{\text{gt} \langle c, s \rangle}) \right) \quad (9.53)$$

$$c \in COU: \quad s \in SEC: \quad \lambda^{\text{GOVERNMENT}^2 \langle c \rangle} p^{\text{imp} \langle c, s \rangle} \left( 1 + tssm^{\text{gov} \langle c, s \rangle} \right) + \lambda^{\text{GOVERNMENT}^1 \langle c, s \rangle} (1 - \alpha^{\text{gt} \langle c, s \rangle}) GM^{\langle c, s \rangle - 1 + \sigma^{\text{arm} \langle c, s \rangle - 1} (-1 + \sigma^{\text{arm} \langle c, s \rangle})} \left( \alpha^{\text{gt} \langle c, s \rangle} GD^{\langle c, s \rangle \sigma^{\text{arm} \langle c, s \rangle - 1} (-1 + \sigma^{\text{arm} \langle c, s \rangle})} \right) \quad (9.54)$$

$$c \in COU: \quad s \in SEC: \quad CD^{\langle c, s \rangle} + DD^{\langle c, s \rangle} + GD^{\langle c, s \rangle} - Y^{\text{home} \langle c, s \rangle} + \sum_{\tilde{s}i \in SEC} ICD^{\langle c, \tilde{s}i, s \rangle} = 0 \quad (9.55)$$

$$c \in COU: \quad s \in SEC: \quad CM^{\langle c, s \rangle} + DM^{\langle c, s \rangle} + GM^{\langle c, s \rangle} - \text{IMPORT}^{\langle c, s \rangle} + \sum_{\tilde{s}i \in SEC} ICM^{\langle c, \tilde{s}i, s \rangle} = 0 \quad (9.56)$$

$$c \in COU: \quad s \in SEC: \quad \pi^{\langle c, s \rangle} - p^{\langle c, s \rangle} Y^{\langle c, s \rangle} \left( 1 - tpral^{\langle c, s \rangle} \right) + p^{\text{k} \langle c \rangle} K^{\langle c, s \rangle} \left( 1 + tf^{\text{k} \langle c, s \rangle} \right) + p^{\text{l} \langle c \rangle} L^{\langle c, s \rangle} \left( 1 + tf^{\text{l} \langle c, s \rangle} \right) + \sum_{\tilde{s}i \in SEC} p^{\langle c, \tilde{s}i \rangle} ICD^{\langle c, s, \tilde{s}i \rangle} \left( 1 + tssd^{\text{prod} \langle c, s, \tilde{s}i \rangle} \right) + \sum_{\tilde{s}i \in SEC} p^{\text{imp} \langle c, \tilde{s}i \rangle} ICM^{\langle c, s, \tilde{s}i \rangle} \quad (9.57)$$

$$c \in COU: \quad s \in SEC: \quad \alpha \in COU: \quad -p^{\text{fob} \langle c, \alpha, s \rangle} + p^{\langle c, s \rangle} \left( 1 + tte^{\langle c, \alpha, s \rangle} \right) = 0 \quad (9.58)$$

$$c \in COU: \quad s \in SEC: \quad \tilde{s}i \in SEC: \quad -\lambda^{\text{FIRM}^4 \langle c, s, \tilde{s}i \rangle} + \alpha^{\text{ict} \langle c, s, \tilde{s}i \rangle} tfp^{\text{y} \langle c, s \rangle} p^{\langle c, s \rangle} \left( 1 - \alpha^{\text{fac} \langle c, s \rangle} \right) \left( 1 - tpral^{\langle c, s \rangle} \right) IC^{\langle c, s \rangle - 1 + \sigma^{\text{y} \langle c, s \rangle - 1} (-1 + \sigma^{\text{y} \langle c, s \rangle})} ICT^{\langle c, s, \tilde{s}i \rangle - 1 + \sigma^{\text{ic} \langle c, s \rangle - 1} (-1 + \sigma^{\text{ic} \langle c, s \rangle})} \left( \alpha^{\text{fac} \langle c, s \rangle} \right) \quad (9.59)$$

$$c \in COU: \quad s \in SEC: \quad \tilde{s}i \in SEC: \quad -ICT^{\langle c, s, \tilde{s}i \rangle} + \left( \alpha^{\text{icd} \langle c, s, \tilde{s}i \rangle} ICD^{\langle c, s, \tilde{s}i \rangle \sigma^{\text{arm} \langle c, \tilde{s}i \rangle - 1} (-1 + \sigma^{\text{arm} \langle c, \tilde{s}i \rangle})} + (1 - \alpha^{\text{icd} \langle c, s, \tilde{s}i \rangle}) ICM^{\langle c, s, \tilde{s}i \rangle \sigma^{\text{arm} \langle c, \tilde{s}i \rangle - 1} (-1 + \sigma^{\text{arm} \langle c, \tilde{s}i \rangle})} \right) \sigma^{\text{arm} \langle c, \tilde{s}i \rangle - 1} (-1 + \sigma^{\text{arm} \langle c, \tilde{s}i \rangle})^{-1} = 0 \quad (9.60)$$

$$c \in COU: \quad s \in SEC: \quad \tilde{s}i \in SEC: \quad -p^{\langle c, \tilde{s}i \rangle} \left( 1 + tssd^{\text{prod} \langle c, s, \tilde{s}i \rangle} \right) + \alpha^{\text{icd} \langle c, s, \tilde{s}i \rangle} \lambda^{\text{FIRM}^4 \langle c, s, \tilde{s}i \rangle} ICD^{\langle c, s, \tilde{s}i \rangle - 1 + \sigma^{\text{arm} \langle c, \tilde{s}i \rangle - 1} (-1 + \sigma^{\text{arm} \langle c, \tilde{s}i \rangle})} \left( \alpha^{\text{icd} \langle c, s, \tilde{s}i \rangle} ICD^{\langle c, s, \tilde{s}i \rangle \sigma^{\text{arm} \langle c, \tilde{s}i \rangle - 1} (-1 + \sigma^{\text{arm} \langle c, \tilde{s}i \rangle})} + (1 - \alpha^{\text{icd} \langle c, s, \tilde{s}i \rangle}) \right) \quad (9.61)$$

$$c \in COU: \quad s \in SEC: \quad \tilde{s}i \in SEC: \quad -p^{\text{imp} \langle c, \tilde{s}i \rangle} \left( 1 + tssm^{\text{prod} \langle c, s, \tilde{s}i \rangle} \right) + \lambda^{\text{FIRM}^4 \langle c, s, \tilde{s}i \rangle} (1 - \alpha^{\text{icd} \langle c, s, \tilde{s}i \rangle}) ICM^{\langle c, s, \tilde{s}i \rangle - 1 + \sigma^{\text{arm} \langle c, \tilde{s}i \rangle - 1} (-1 + \sigma^{\text{arm} \langle c, \tilde{s}i \rangle})} \left( \alpha^{\text{icd} \langle c, s, \tilde{s}i \rangle} ICD^{\langle c, s, \tilde{s}i \rangle \sigma^{\text{arm} \langle c, \tilde{s}i \rangle - 1} (-1 + \sigma^{\text{arm} \langle c, \tilde{s}i \rangle})} \right) \quad (9.62)$$

$$c \in COU: \quad s \in SECT: \quad \text{TRANS}^{\text{total} \langle c \rangle} - Y^{\langle c, s \rangle} + Y^{\text{home} \langle c, s \rangle} + \sum_{\alpha \in COU} EX^{\langle c, \alpha, s \rangle} = 0 \quad (9.63)$$

$$c \in COU: \quad s \in SECT: \quad -Y^{\langle c, s \rangle} + Y^{\text{home} \langle c, s \rangle} + \sum_{\alpha \in COU} EX^{\langle c, \alpha, s \rangle} = 0 \quad (9.64)$$

$$c \in COU_{\text{big}}: \quad s \in SEC: \quad -\text{IMPORT}^{\langle c, s \rangle} + \theta^{\text{im} \langle c, s \rangle} \left( \sum_{\alpha \in COU} \alpha^{\text{im} \langle \alpha, c, s \rangle} \left( \text{scale}^{\langle c \rangle - 1} \text{scale}^{\langle \alpha \rangle} \text{IM}^{\langle \alpha, c, s \rangle} \left( 1 + i\text{berg}^{\text{cost} \langle \alpha, c, s \rangle} \right) \right) \sigma^{\text{im} \langle s \rangle - 1} (-1 + \sigma^{\text{im} \langle s \rangle}) \right) \sigma^{\text{im} \langle s \rangle} (-1 + \sigma^{\text{im} \langle s \rangle})^{-1} = 0 \quad (9.65)$$

$$c \in COUbig: \quad s \in SEC: \quad \pi^{imp\langle c,s \rangle} + scale\langle c \rangle^{-1} \left( \sum_{\alpha \in COU} scale\langle \alpha \rangle p^{cif\langle \alpha,c,s \rangle} IM\langle \alpha,c,s \rangle \left( 1 + trm\langle \alpha,c,s \rangle \right) \right) - p^{imp\langle c,s \rangle} IMPORT\langle c,s \rangle = 0 \quad (9.66)$$

$$c \in COUbig: \quad s \in SEC: \quad \alpha \in COU: \quad EX\langle \alpha,c,s \rangle - IM\langle \alpha,c,s \rangle = 0 \quad (9.67)$$

$$c \in COUbig: \quad s \in SEC: \quad \alpha \in COU: \quad -scale\langle c \rangle^{-1} scale\langle \alpha \rangle p^{cif\langle \alpha,c,s \rangle} \left( 1 + trm\langle \alpha,c,s \rangle \right) + \alpha^{im\langle \alpha,c,s \rangle} scale\langle c \rangle^{-1} scale\langle \alpha \rangle \theta^{im\langle c,s \rangle} p^{imp\langle c,s \rangle} \left( 1 + idery^{cost\langle \alpha,c,s \rangle} \right) \left( scale\langle c \rangle^{-1} scale\langle \alpha \rangle IM\langle \alpha,c,s \rangle \left( 1 + idery^{cost\langle \alpha,c,s \rangle} \right) \right)^{-1} = 0 \quad (9.68)$$

$$c \in COUbig: \quad s \in SEC: \quad \alpha \in COU: \quad p^{fob\langle c,\alpha,s \rangle} - p^{cif\langle c,\alpha,s \rangle} + \tau\langle c,\alpha,s \rangle p^{trans} = 0 \quad (9.69)$$

$$c \in COUonly: \quad s \in SEC: \quad -IMPORT\langle c,s \rangle + \theta^{im\langle c,s \rangle} \left( \sum_{\alpha \in COU \setminus c} \alpha^{im\langle \alpha,c,s \rangle} \left( scale\langle c \rangle^{-1} scale\langle \alpha \rangle IM\langle \alpha,c,s \rangle \left( 1 + idery^{cost\langle \alpha,c,s \rangle} \right) \right)^{\sigma^{im\langle s \rangle} - 1} \left( -1 + \sigma^{im\langle s \rangle} \right) \right)^{\sigma^{im\langle s \rangle} \left( -1 + \sigma^{im\langle s \rangle} \right)^{-1}} = 0 \quad (9.70)$$

$$c \in COUonly: \quad s \in SEC: \quad \pi^{imp\langle c,s \rangle} + scale\langle c \rangle^{-1} \left( \sum_{\alpha \in COU} scale\langle \alpha \rangle p^{cif\langle \alpha,c,s \rangle} IM\langle \alpha,c,s \rangle \left( 1 + trm\langle \alpha,c,s \rangle \right) \right) - p^{imp\langle c,s \rangle} IMPORT\langle c,s \rangle = 0 \quad (9.71)$$

$$c \in COUonly: \quad s \in SEC: \quad -scale\langle c \rangle IM\langle c,c,s \rangle = 0 \quad (9.72)$$

$$c \in COUonly: \quad s \in SEC: \quad \alpha \in COU: \quad EX\langle \alpha,c,s \rangle - IM\langle \alpha,c,s \rangle = 0 \quad (9.73)$$

$$c \in COUonly: \quad s \in SEC: \quad \alpha \in COU: \quad p^{fob\langle c,\alpha,s \rangle} - p^{cif\langle c,\alpha,s \rangle} + \tau\langle c,\alpha,s \rangle p^{trans} = 0 \quad (9.74)$$

$$c \in COUonly: \quad s \in SEC: \quad \alpha \in COU \setminus c: \quad -scale\langle c \rangle^{-1} \left( \sum_{\alpha' \in COU} \delta\langle \alpha,\alpha' \rangle scale\langle \alpha' \rangle p^{cif\langle \alpha',c,s \rangle} \left( 1 + trm\langle \alpha',c,s \rangle \right) \right) + \alpha^{im\langle \alpha,c,s \rangle} scale\langle c \rangle^{-1} scale\langle \alpha \rangle \theta^{im\langle c,s \rangle} p^{imp\langle c,s \rangle} \left( 1 + idery^{cost\langle \alpha,c,s \rangle} \right) \left( scale\langle c \rangle^{-1} scale\langle \alpha \rangle IM\langle \alpha,c,s \rangle \left( 1 + idery^{cost\langle \alpha,c,s \rangle} \right) \right)^{-1} = 0 \quad (9.75)$$

## 10 Parameter settings

$$\alpha^{im\langle COU1,COU1,SEC1 \rangle} = 0 \quad (10.1)$$

$$\alpha^{im\langle COU1,COU1,SEC2 \rangle} = 0 \quad (10.2)$$

$$\alpha^{im\langle COU1,COU1,SEC3 \rangle} = 0 \quad (10.3)$$

$$\alpha^{im\langle COU1,COU1,SEC4 \rangle} = 0 \quad (10.4)$$

$$\alpha^{im\langle COU1,COU1,SEC5 \rangle} = 0 \quad (10.5)$$



$$\alpha^{\text{im}\langle\text{COU1,COU1,SEC6}\rangle} = 0 \quad (10.6)$$

$$\alpha^{\text{im}\langle\text{COU1,COU1,SEC7}\rangle} = 0 \quad (10.7)$$

$$\alpha^{\text{im}\langle\text{COU1,COU1,SEC8}\rangle} = 0 \quad (10.8)$$

$$\alpha^{\text{im}\langle\text{COU2,COU2,SEC1}\rangle} = 0 \quad (10.9)$$

$$\alpha^{\text{im}\langle\text{COU2,COU2,SEC2}\rangle} = 0 \quad (10.10)$$

$$\alpha^{\text{im}\langle\text{COU2,COU2,SEC3}\rangle} = 0 \quad (10.11)$$

$$\alpha^{\text{im}\langle\text{COU2,COU2,SEC4}\rangle} = 0 \quad (10.12)$$

$$\alpha^{\text{im}\langle\text{COU2,COU2,SEC5}\rangle} = 0 \quad (10.13)$$

$$\alpha^{\text{im}\langle\text{COU2,COU2,SEC6}\rangle} = 0 \quad (10.14)$$

$$\alpha^{\text{im}\langle\text{COU2,COU2,SEC7}\rangle} = 0 \quad (10.15)$$

$$\alpha^{\text{im}\langle\text{COU2,COU2,SEC8}\rangle} = 0 \quad (10.16)$$

$$\phi^{\langle\text{COU1}\rangle} = 0.25 \quad (10.17)$$

$$\phi^{\langle\text{COU2}\rangle} = 0.25 \quad (10.18)$$

$$\phi^{\langle\text{COU3}\rangle} = 0.25 \quad (10.19)$$

$$\phi^{\langle\text{COU4}\rangle} = 0.25 \quad (10.20)$$

$$L^{\text{slack}\langle\text{COU1}\rangle} = 0 \quad (10.21)$$

$$L^{\text{slack}\langle\text{COU2}\rangle} = 0 \quad (10.22)$$

$$L^{\text{slack}\langle\text{COU3}\rangle} = 0 \quad (10.23)$$

$$L^{\text{slack}\langle\text{COU4}\rangle} = 0 \quad (10.24)$$